

Lesson Check Answers

1. Gases are easily compressed because of the space between gas particles.
2. temperature, pressure, and amount of gas
3. Because the gas in the inflated air bag can be compressed, the bag absorbs some of the energy from the impact of a collision. The solid steering wheel cannot do this.
4. If the temperature decreases, the pressure will also decrease.
5. The volume would need to increase by a factor of four.
6. Increase the amount of gas in the container a hundredfold.
7. Sample answer: The pressure of the gas inside the sprayer is greater than atmospheric pressure. As the gas propels the contents out, the number of gas particles in the sprayer decreases and the gas pressure decreases.
8. **BIG IDEA** According to kinetic theory, the particles in a gas have insignificant volume, and the distance between particles in a gas is much greater than the distance between particles in a liquid or solid. Under pressure, the particles in a gas are forced closer together, resulting in a smaller overall volume.

Sample Problems

$$P_1V_1 = P_2V_2 \quad \text{Boyle's Law}$$

$$V_2 = P_1V_1 / P_2$$

$$\begin{aligned} 9. \quad 105 \text{ kPa} \times 2.50 \text{ L} &= 40.5 \text{ kPa} \times V_2 \\ V_2 &= 105 \text{ kPa} \times 2.50 \text{ L} / 40.5 \text{ kPa} = 6.48 \text{ L} \end{aligned}$$

$$P_1 = P_2V_2 / V_1$$

$$\begin{aligned} 10. \quad 205 \text{ kPa} \times 4.00 \text{ L} &= P_2 \times 12.0 \text{ L} \\ P_2 &= 205 \text{ kPa} \times 4.00 \text{ L} / 12.0 \text{ L} = 68.3 \text{ kPa} \end{aligned}$$

$$V_1 / T_1 = V_2 / T_2 \quad \text{Charles's Law}$$

Must use K temperature

$$V_2 = T_2 V_1 / T_1$$

- 11.** $T_1 = 325^\circ\text{C} + 273 = 598 \text{ K}$
 $T_2 = 25^\circ\text{C} + 273 = 298 \text{ K}$
 $6.80 \text{ L}/598 \text{ K} = V_2/298 \text{ K}$
 $V_2 = 298 \text{ K} \times 6.80 \text{ L}/598 \text{ K} = 3.39 \text{ L}$
- 12.** $T_1 = -50.0^\circ\text{C} + 273 = 223 \text{ K}$
 $T_2 = 100.0^\circ\text{C} + 273 = 373 \text{ K}$
 $5.00 \text{ L}/223 \text{ K} = V_2/373 \text{ K}$
 $V_2 = 373 \text{ K} \times 5.00 \text{ L}/223 \text{ K} = 8.36 \text{ L}$

$$P_1 / T_1 = P_2 / T_2 \quad \text{Gay-Lussac's Law}$$

Must use K temperature

$$P_2 = P_1 T_2 / T_1$$

- 13.** $T_1 = 41^\circ\text{C} + 273 = 314 \text{ K}$
 $T_2 = 22^\circ\text{C} + 273 = 295 \text{ K}$
 $108 \text{ kPa}/314 \text{ K} = P_2/295 \text{ K}$
 $P_2 = 295 \text{ K} \times 108 \text{ kPa}/314 \text{ K} = 101 \text{ kPa}$

$$P_1 / T_1 = P_2 / T_2 \quad \dots \quad T_2 = P_2 T_1 / P_1$$

- 14.** $T_1 = 27^\circ\text{C} + 273 = 300 \text{ K}$
 $198 \text{ kPa}/300 \text{ K} = 225 \text{ kPa}/T_2$
 $T_2 = 225 \text{ kPa} \times 300 \text{ K}/198 \text{ kPa} = 341 \text{ K} (68^\circ\text{C})$

$$P_1V_1 / T_1 = P_2V_2 / T_2 \quad \text{Combined Gas Law}$$

Must use K temperature

$$V_2 = P_1 V_1 T_2 / P_2 T_1$$

$$\begin{aligned} 15. \quad T_1 &= 25^\circ\text{C} + 273 = 298 \text{ K} \\ T_2 &= 125^\circ\text{C} + 273 = 398 \text{ K} \\ 155 \text{ kPa} \times 1.00 \text{ L} / 298 \text{ K} &= 605 \text{ kPa} \times V_2 / 398 \text{ K} \\ V_2 &= 398 \text{ K} \times 155 \text{ kPa} \times 1.00 \text{ L} / (298 \text{ K} \\ &\times 605 \text{ kPa}) = 0.342 \text{ L} \end{aligned}$$

$$P_2 = P_1 V_1 T_2 / V_2 T_1$$

$$\begin{aligned} 16. \quad T_1 &= -50^\circ\text{C} + 273 = 223 \text{ K} \\ T_2 &= 102^\circ\text{C} + 273 = 375 \text{ K} \\ 107 \text{ kPa} \times 5.00 \text{ L} / 223 \text{ K} &= P_2 \times 7.00 \text{ L} / 375 \text{ K} \\ P_2 &= 375 \text{ K} \times 107 \text{ kPa} \times 5.00 \text{ L} / (223 \text{ K} \times 7.00 \text{ L}) \\ &= 1.29 \times 10^2 \text{ kPa} \end{aligned}$$

Lesson Check Answers

17. At constant temperature, volume decreases as pressure increases.
18. At constant pressure, volume increases as temperature increases.
19. At constant volume, pressure increases as temperature increases.
20. The combined gas law allows you to do calculations when the only constant is the amount of gas.
21. $P_1 \times V_1 = P_2 \times V_2$; P_1 = initial pressure; V_1 = initial volume; P_2 = final pressure; V_2 = final volume
22. $P_1V_1 = P_2V_2$ Boyle's Law
 $V_2 = P_1V_1 / P_2$
 $V_2 = 101 \text{ kPa} \times 6.00 \text{ L} / 25.0 \text{ kPa}$
 $V_2 = 24.2 \text{ L}$
23. When the pressure is constant, $P_1 = P_2$, so the pressure terms cancel, leaving an equation for Charles's law.
24. The outside pressure decreases, causing a greater increase in the balloon's volume.
25. **BIG IDEA** As temperatures decrease toward absolute zero, particles in the gas slow down, and attractions between particles increase. A gas would liquefy and then solidify as it cooled to temperatures near absolute zero.

Sample Problems

26. $PV = nRT$ Ideal Gas Law ... **$n = PV/RT$**
 $R = 8.31 \text{ L}\cdot\text{kPa}/\text{K}\cdot\text{mol}$ based on the units given for the other variables

$$n = 1.89 \times 10^3 \text{ kPa} \times 685 \text{ L} / 8.31 \text{ L}\cdot\text{kPa}/\text{K}\cdot\text{mol} \times 621 \text{ K}$$
$$n = 2.51 \times 10^2 \text{ moles He}$$

27. $PV = nRT$ Ideal Gas Law ... **$P = nRT/V$**
Must use K temperature
 $R = 8.31 \text{ L}\cdot\text{kPa}/\text{K}\cdot\text{mol}$ based on the units given for the other variables

$$P = 0.450 \text{ mol} \times 8.31 \text{ L}\cdot\text{kPa}/\text{K}\cdot\text{mol} \times (273 + 25) \text{ K} / 0.650 \text{ L}$$
$$P = 1.71 \times 10^3 \text{ kPa}$$

28. $PV = nRT$ Ideal Gas Law ... **$n = PV/RT$**
Must use K temperature
 $R = 8.31 \text{ L}\cdot\text{kPa}/\text{K}\cdot\text{mol}$ based on the units given for the other variables

$$n = 102 \text{ kPa} \times 2.20 \text{ L} / 8.31 \text{ L}\cdot\text{kPa}/\text{K}\cdot\text{mol} \times (273 + 37) \text{ K}$$
$$n = 0.087 \text{ moles Air} \times 29 \text{ g/mol} = 2.5 \text{ g Air}$$

29. $PV = nRT$ Ideal Gas Law ... **$V = nRT/P$**
Must use K temperature
 $R = 8.31 \text{ L}\cdot\text{kPa}/\text{K}\cdot\text{mol}$ based on the units given for the other variables

$$12 \text{ g} \times 1 \text{ mol}/32 \text{ O}_2 = 0.375 \text{ mol}$$
$$V = 0.375 \text{ mol} \times 8.31 \text{ L}\cdot\text{kPa}/\text{K}\cdot\text{mol} \times (273 + 25) \text{ K} / 52.7 \text{ kPa}$$
$$V = 17.6 \text{ L}$$

Lesson Check Answers

30. by using the equation for the ideal gas law ($PV = nRT$)
31. Real gases deviate from ideal behavior at low temperatures and high pressures.
32. 17.0 L
33. 4.48 kg
34. An ideal gas obeys the assumptions of kinetic theory. A real gas deviates from ideal behavior except within a small range of conditions.
35. The nitrogen molecule is nonpolar and the ammonia molecule is polar. So there are stronger intermolecular attractions in ammonia.
36. **BIG IDEA** In real gases, there are attractions between molecules, and the molecules have volume. At low temperatures, attractions between molecules pull them together and reduce the volume. At high pressures, the volume occupied by the molecules is a significant part of the total volume.

32. $PV = nRT$ Ideal Gas Law ... $V = nRT/P$

Must use K temperature

$R = 8.31 \text{ L}\cdot\text{kPa}/\text{K}\cdot\text{mol}$ based on the units given for the other variables

$$V = 0.582 \text{ mol} \times 8.31 \text{ L}\cdot\text{kPa}/\text{K}\cdot\text{mol} \times (273 + 15) \text{ K} / 81.9 \text{ kPa}$$

$$V = 17.1 \text{ L}$$

33. $PV = nRT$ Ideal Gas Law ... $n = PV/RT$

Must use K temperature

$R = 8.31 \text{ L}\cdot\text{kPa}/\text{K}\cdot\text{mol}$ based on the units given for the other variables

$$n = 2.00 \times 10^4 \text{ kPa} \times 20.0 \text{ L} / 8.31 \text{ L}\cdot\text{kPa}/\text{K}\cdot\text{mol} \times (273 + 28) \text{ K}$$

$$n = 159.9 \text{ moles } \text{N}_2 \text{ (g)} \times 28 \text{ g/mol} = 4478 \text{ g} = 4.48 \text{ kg } \text{N}_2 \text{ (g)}$$

Sample Problems

Figure 14.6 The ratios are equal

37. Dalton's Law of Partial Pressure $\rightarrow P_{\text{total}} = P_{\text{O}_2} + P_{\text{N}_2} + P_{\text{CO}_2}$

$$P_{\text{CO}_2} = P_{\text{total}} - (P_{\text{O}_2} + P_{\text{N}_2})$$

37. $32.9 \text{ kPa} - 6.6 \text{ kPa} - 23.0 \text{ kPa} = 3.3 \text{ kPa}$

38. $20.0 \text{ kPa} + 46.7 \text{ kPa} + 26.7 \text{ kPa} = 93.4 \text{ kPa}$, or
 $9.34 \times 10^1 \text{ kPa}$

39. Graham's Law of Diffusion/Effusion

$$\text{Rate H}_2(\text{g}) / \text{Rate CO}_2(\text{g}) = \sqrt{(\text{molar mass CO}_2)} / \sqrt{(\text{molar mass H}_2)}$$

$$\text{Rate H}_2(\text{g}) / \text{Rate CO}_2(\text{g}) = \sqrt{(44.0 \text{ g/mol})} / \sqrt{(2.00 \text{ g/mol})}$$

$$\text{Rate H}_2(\text{g}) / \text{Rate CO}_2(\text{g}) = 6.6 / 1.4 = 4.7 / 1$$

40. Total pressure is equal to the sum of the partial pressures of the components.

41. Gases with lower molar masses diffuse and effuse faster than gases with higher molar masses.

42. Subtract the partial pressures of the other gases from the total pressure.

43. 191.3 kPa

44. During effusion, a gas escapes through a tiny hole in its container. In both cases, the rate depends on the molar mass.

45. Carbon monoxide and nitrogen have almost identical molar masses when the masses are rounded to two significant figures (28 g).

46. Both tables report data for dry air as mainly nitrogen and oxygen. Table 14.1 uses percents and includes a compound. The table on R1 uses ppm and provides specific data for elements.

43. Dalton's Law of Partial Pressure $\rightarrow P_{\text{total}} = P_{\text{O}_2} + P_{\text{N}_2} + P_{\text{CO}_2} + P_{\text{others}}$

$$P_{\text{N}_2} = P_{\text{total}} - (P_{\text{O}_2} + P_{\text{CO}_2} + P_{\text{others}})$$

$$P_{\text{N}_2} = 245.0 \text{ kPa} - 51.3 \text{ kPa} - 0.10 \text{ kPa} - 2.3 \text{ kPa} = 191.3 \text{ kPa}$$